

Mathematics:

ALGEBRA



LINEAR EQUATIONS

Slope-intercept form

$$y = mx + b \quad m = \frac{y_2 - y_1}{x_2 - x_1}$$

Standard form

$$Ax + By = C \quad m = -\frac{A}{B}$$

POLAR COORDINATES

(x, y) to (r, θ)

$$x^2 + y^2 = r^2$$

$$\tan \theta = \frac{y}{x}$$

(r, θ) to (x, y)

$$y = r \sin \theta$$

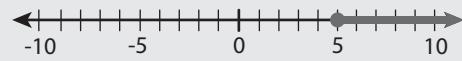
$$x = r \cos \theta$$

$$(x, y) = (r \cos \theta, \sin \theta)$$

INEQUALITIES

greater than or equal to

$$x \geq 5$$



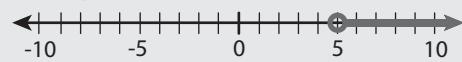
less than or equal to

$$x \leq 5$$



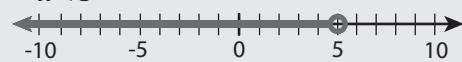
greater than

$$x > 5$$



less than

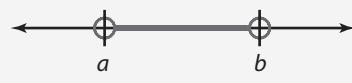
$$x < 5$$



COMPOUND INEQUALITIES

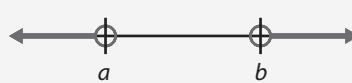
Intersection

$$a \leq x \leq b$$



Union

$$a < x \text{ or } x > b$$



QUADRATIC EQUATIONS

Standard form

$$y = ax^2 + bx + c$$

axis of symmetry: $x = -\frac{b}{2a}$

vertex: $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$

Vertex form

$$y = a(x - h)^2 + k$$

axis of symmetry: $x = h$

vertex: (h, k)

TRANSFORMING FUNCTIONS

$$y = -f(x) \quad \text{reflection across the } x\text{-axis (vertical reflection)}$$

$$y = f(x) + k \quad \text{vertical shift up } k \text{ units } (k > 0) \text{ or down } k \text{ units } (k < 0)$$

$$y = kf(x) \quad \text{vertical stretch (if } k > 1\text{) or compression (if } k < 1\text{)}$$

$$y = f(-x) \quad \text{reflection across the } y\text{-axis (horizontal reflection)}$$

$$y = f(x + k) \quad \text{horizontal shift right } k \text{ units } (k < 0) \text{ or left } k \text{ units } (k > 0)$$

$$y = f(kx) \quad \text{horizontal stretch } (k < 1) \text{ or compression } (k > 1)$$

GROWTH AND DECAY

Growth

$$A = P(1 + r)^t$$

Decay

$$A = P(1 - r)^t$$

Compound Interest

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

A = final amount

P = initial amount

r = interest rate

t = time period

n = number of times

interest is compounded
in a time period

DISTRIBUTING AND FACTORING

$$3x(7xy - z^3) \quad \begin{array}{c} \text{Distribute} \\ \curvearrowright \\ \text{Factor} \end{array} \quad 21x^2y - 3xz^3$$

- $a^2 - b^2 = (a + b)(a - b)$
- $a^2 + 2ab + b^2 = (a + b)(a + b) = (a + b)^2$
- $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
- $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

PROPERTIES OF LOGARITHMS

$$\log_b(m) = \frac{\log(m)}{\log(b)}$$

$$\log_b(mn) = \log_b(m) + \log_b(n)$$

$$\log_b\left(\frac{m}{n}\right) = \log_b(m) - \log_b(n)$$

$$\log_b(m^n) = n \times \log_b(m)$$

QUADRATIC FORMULA

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

LOGARITHMS

$$y = \log_b x \rightarrow b^y = x$$

$$\log x = \log_{10} x$$

$$\ln x = \log_e x$$

HORIZONTAL ASYMPTOTES

For polynomials with first terms $\frac{ax^n}{bx^d} \dots$

$n < d$ The x -axis ($y = 0$) is a horizontal asymptote.

$n = d$ There is a horizontal asymptote at $y = \frac{a}{b}$.

$n > d$ There is no horizontal asymptote.

MATRIX DETERMINANTS

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$$

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$

$$= a(ei - fh) - b(di - fg) + c(dh - eg)$$

AREA OF A TRIANGLE

$$\mathbf{A} = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$